

# the complexity of predicting atomicity violations

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# Motivation: Interleaving explosion problem

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- Testing is the main technique for correctness in the industry
- Fundamentally challenged for concurrent programs:
  - Given even a *single* test input for a concurrent program, testing is hard!
  - Too many interleavings to check thoroughly

**Idea: Select a small subset of interleavings to test that are likely to expose concurrency bugs**

# How to select schedules cleverly

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- CHES: Microsoft Research

*Explores all possible interleavings with at most  $k$  context-switches, for a small  $k$ .*

*We believe atomicity errors will constitute a far smaller but more interesting class of runs to test.*

- A bunch of tools that try to somehow come up with interleavings that may have errors

- Eg. ConTest: IBM

- Our view:

Don't look randomly for schedules!

Look systematically for interesting patterns of thread interaction that are more likely to have errors.

# In this talk: Atomicity

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## *Atomicity :*

One particular high-level pattern that gets violated in many concurrency bugs:

- A local piece of code needs to access shared data without (real) interference from other threads.
- Extremely common intention, the violation of which leads to many errors.
- In concurrency bug studies, we as well as others ([Lu-Park-Seo-Zhou'08](#)) have found that the majority of errors (~70%) are due to atomicity violations.
- Hence finding executions that violate atomicity and testing them is a good way to prune the interleavings to test!

# Atomicity error: example

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- [https://bugzilla.mozilla.org/show\\_bug.cgi?id=290446](https://bugzilla.mozilla.org/show_bug.cgi?id=290446)
- Summary:
  - Update of remote calendar does not use WebDAV locking (concurrency control)
- When updating/inserting a new event in a remote WebDAV calendar, the calendar file is not locked. In order to avoid losing data the concurrency control of WebDAV should be used (Locking).
- Steps to Reproduce:
  - 1. User A starts creating a new event in the remote calendar
  - 2. User B starts creating a new event in the remote calendar
  - 3. Users A and B read-modify-write operations are interleaved incorrectly
- Actual Results: The actual sequence could/would be: 1. User A - GET test.ics 2. User B - GET test.ics 3. User A - PUT test.ics 4. User B - PUT test.ics
- *In this case the new event posted by user A is lost.*

# Atomicity

- **Transaction**: sequential logical unit of computation:  
syntactically identified: small methods, procedures, etc.
- An execution  $r$  of a concurrent program  $P$  is **atomic** if there exists an **equivalent** run of  $P$  in which **every transaction** is **non-interleaved**.

execution

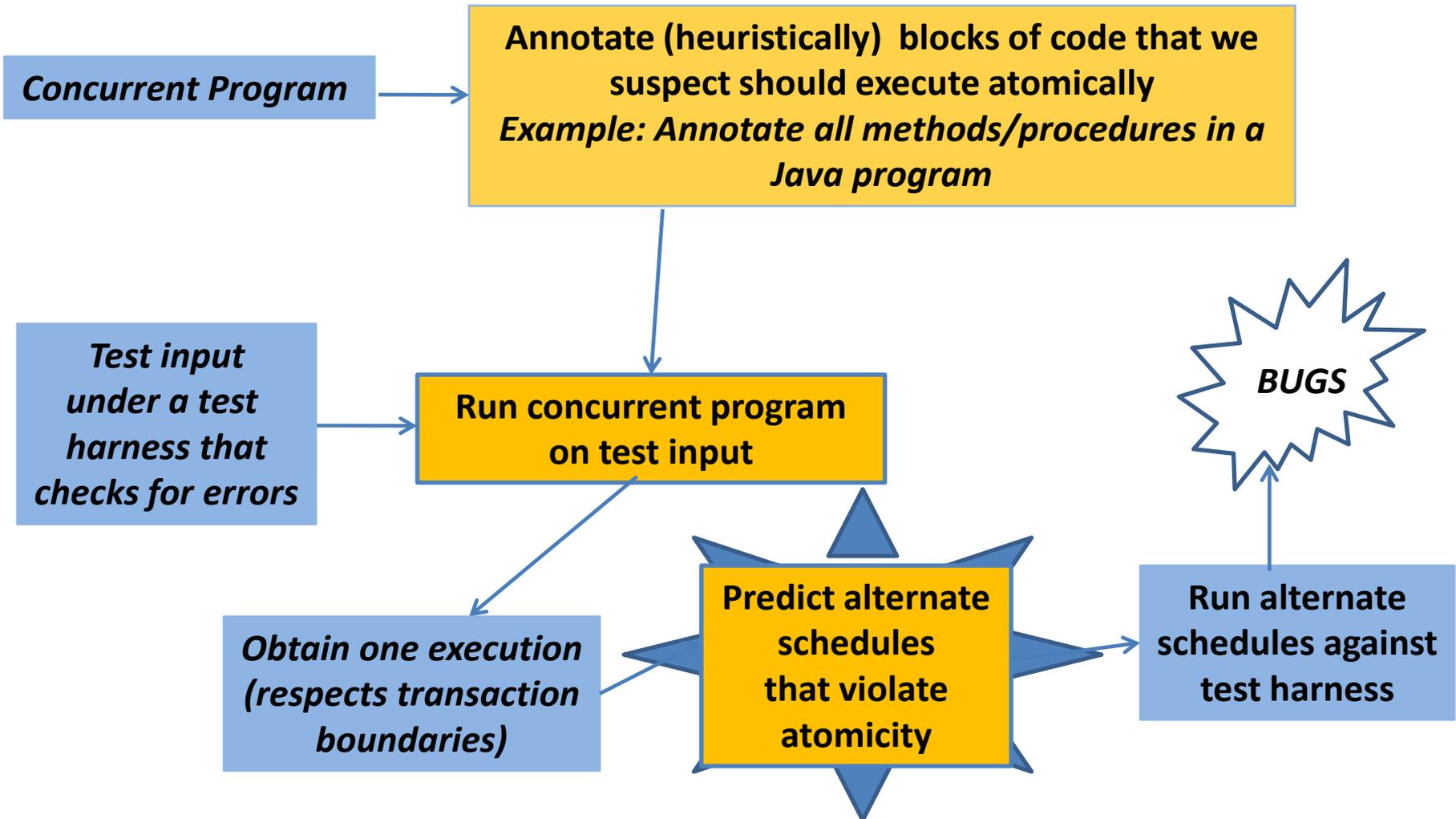


equivalent  
serial execution



# Application: Finding bugs while testing

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# Main problem

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- Given programs  $P_1 \parallel P_2 \parallel \dots \parallel P_n$  where
  - Each  $P_i$  is be a straight-line program  
(useful when attacking the testing problem)
  - Each  $P_i$  is be a regular program  
(modeled as finite automata; useful in abstracted pgms)
  - Each  $P_i$  is a recursive program  
(modeled as PDS; for abstracted pgms with recursion)

## Question:

Is there any interleaved run that violates atomicity?

# Atomicity based on Serializability;

## When are two runs equivalent?

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Events:  $\{ T:\text{begin}, T:\text{end} \} \cup \{ T:\text{read}(x), T:\text{write}(x) \mid x \text{ is a shared var} \}$

Concurrent Run: sequence of events.

Dependence/  
Conflicting events:  $\mathcal{D} = \{(T_1 : a_1, T_2 : a_2) \mid T_1 = T_2 \vee \exists x \exists i, j \in \{1, 2\} : a_i = \text{write}(x) \wedge a_j \in \{\text{read}(x), \text{write}(x)\}\}$

Equivalence of Runs: two runs are equivalent if conflicting events are not reordered

$r \sim r'$  iff for every  $e_1 D e_2$ ,  $r \downarrow \{e_1, e_2\} = r' \downarrow \{e_1, e_2\}$

Serial Run: all transactions are executed **non-interleaved**.

Atomic (Serializable) Run: there exists an **equivalent** serial run.

# Atomicity based on Serializability

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T1: 

T1: read(x)

T1: read (y)

T2: 

T2: write(y)

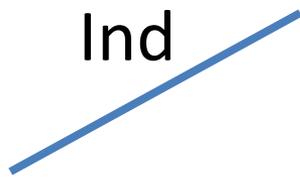
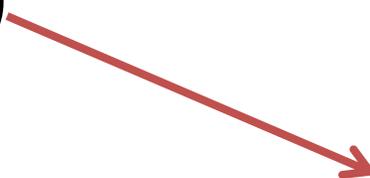
T2: write(x)

T2: 

Ind

T1: write(z1)

T1: 



# Atomicity based on Serializability

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T1: 

T1: read(x)

T1: read (y)

T1: write(z1)

T1: 

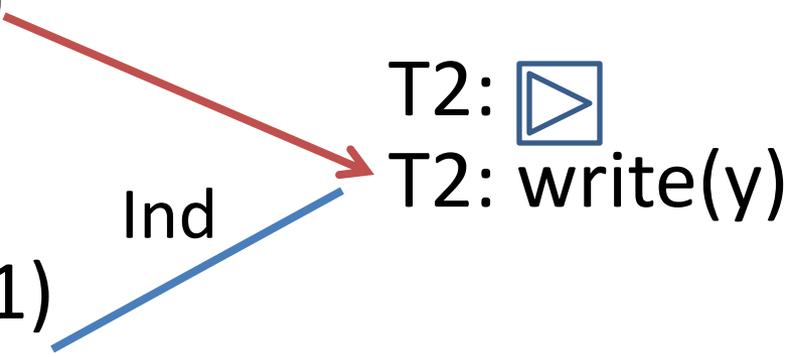
T2: 

T2: write(y)

T2: write(x)

T2: 

Ind



# Atomicity based on Serializability

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T1: 

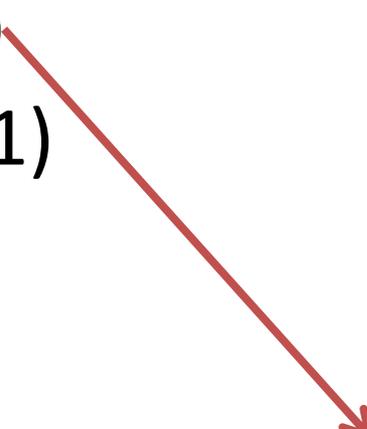
T1: read(x)

T1: read (y)

T1: write(z1)

T1: 

T2: 

 T2: write(y)

T2: write(x)

T2: 

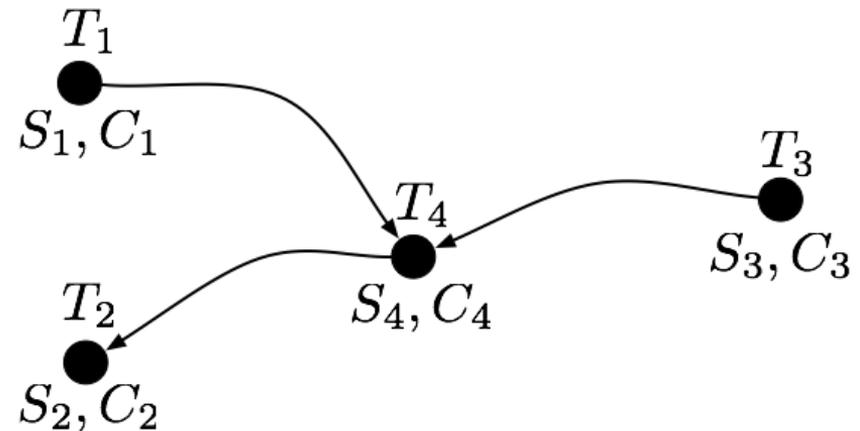
# Before we predict, can we monitor atomicity efficiently?

- Monitoring: Given an execution  $r$ , is  $r$  atomic?

- An extremely satisfactory solution  
[Farzan-Madhusudan: CAV08]

We can build sound and complete monitoring algorithms that keeps track of:

- a set of vars for each thread
- a graph with vertices as threads



- If #vars =  $V$ , # threads =  $n$ , then algorithm uses  $O(n^2 + nV)$  space.

Efficient streaming algorithm.

*Independent of length of run!*

# Predicting Atomicity Violations

## Example:

Given programs  
P1 and P2  
(here straight-line)  
check whether  
there is an  
interleaving that  
violates  
atomicity.

**P1:** T1: begin  
T1: acq (l)  
T1: read(Amount)  
T1: rel (l)  
T1: acq(l)  
T1: write(Amount)  
T1: rel(l)  
T1: end

**P2:** T2: begin  
T2: acq (l)  
T2: read(Amount)  
T2: rel (l)  
T2: acq(l)  
T2: write(Amount)  
T2: rel(l)  
T2: end

T1: begin  
T1: acq (l)  
T1: read(Amount)  
T1: rel (l)

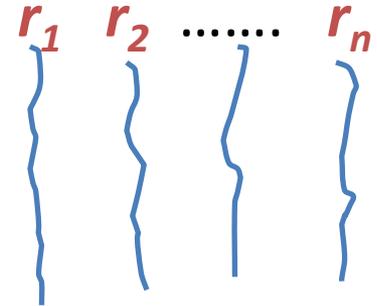
T2: begin  
T2: acq (l)  
T2: read(Amount)  
T2: rel (l)  
T2: acq(l)  
T2: write(Amount)  
T2: rel(l)  
T2: end

T1: acq(l)  
T1: write(Amount)  
T1: rel(l)  
T1: end

Interleaved execution of P1 and P2  
that violates atomicity

# Prediction Model

- Given an execution  $r$ , look at the local executions each thread executes  $r_1, r_2, \dots, r_n$
- Can we find another execution  $r'$  that is obtained by recombining this set of local runs such that  $r'$  is non-atomic?
- Predicted runs could
  - respect no synchronization constraints (less accurate)
  - respect concurrency control constraints such as locking (more accurate)
- The run  $r'$  may not be actually feasible!
  - Conditionals in programs may lead the program to different code
  - Certain operations on datastructures may disable other operations ....
- **Key requirement:**  
*We should not enumerate all interleavings!*  
*Must be more efficient.*



# Predicting atomicity violations

How to predict atomicity violations for st-line or regular programs?

- **Naïve algorithm:**

- Explore all interleavings and monitor each for atomicity violations
- Runs in time  $O(k^n)$  for n-length runs and k threads --- infeasible in practice!

- **Better algorithm: Dynamic programming using the monitoring algm**

- *Predicting from a single run with a constant number of variables, can be done in time*

$$O(n^k 2^{k^2}) \quad \text{---- better than } n^k, \text{ the number of interleavings}$$

*But even  $n^k$  is huge! Too large to work in practice even for  $k=2$ !*

*(m is 100 million events!  $k=2,..10,..$ )*

*Also, exponential dependence in k is unavoidable (problem is NP-hard).*

- *We want to avoid the k being on the exponent of m*

*Main question of the paper: Can we solve in time linear in m? (like  $n+2^k$ )*

*i.e. can we remove the exponent k from n?*

# Main results - I

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- **Good news:**

If prediction need not respect any synchronization constraint (no locks)

- *Predicting from a single run with a constant number of variables, can be done in time*

$$O(n + kc^k) \quad n=\text{length of runs}; \quad k = \# \text{ threads}$$

- *Regular programs also can be solved in time  $O(n + kc^k)$  where  $n$ =size of each local program,  $k$  = #threads*

- *Recursive programs are also (surprisingly) decidable.*

$$O(n^3 + kc^k)$$

*where  $n$ =size of each local program,  $k$  = #threads*

# Main results - II

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- **Bad news:**

If prediction *needs to respect locking*,  
existence of prediction algorithm for regular programs  
running in time linear in  $m$  is **unlikely**.

In fact, algorithms for regular programs that take time a fixed  
polynomial in  $n$  is unlikely.

i.e.  $O(\text{poly}(m) \cdot f(k))$  for **any** function  $f()$  is unlikely!

The problem is **W[1]-hard**.

- Also, prediction for concurrent recursive programs in the presence of locks is undecidable.

# Prediction without synchronization constraints

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- Idea: Compositional reasoning
  - Extract from each local thread run a small amount of information (in time linear in the run)
  - Combine the information across threads to check for atomicity violations
  - Information needed from each local run is called a *profile*.

# Profiles

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- *Key idea:*

*If there is a serializability violation, then there are really only two events in each thread that are important!*

*Also, we need to know if these events occur in the same transaction or not.*

Let  $r$  be a local run of a thread  $T$ .

*Profiles of  $r$  are:*

- $T:\text{beg } T:a \ T:\text{end}$  event  $a$  occurs in  $r$
- $T:\text{beg } T:a \ T:b \ T:\text{end}$   $a$  occurs followed by  $b$  within the *same transaction*
- $T:\text{beg } T:a \ T:\text{end } T:\text{beg } T:b \ T:\text{end}$   $a$  occurs followed by  $b$  but in *different transactions*

# Reasoning atomicity using profiles

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## Key lemma:

A set of programs with no locks (straight-line, regular or recursive) has a non-serializable execution *iff*

there is a profile of each local program such that the profiles, viewed as a program, have a non-serializable execution.

**Proof idea:** skeleton of a serializability violation:

**Only two events  
per thread are needed  
to witness “cycle” for  
non-serializability**

# Prediction without synchronization constraints

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- Straight-line and regular programs:  $O(n+kc^k)$  time
  - Extract profiles from each local program
    - $O(n)$  time --- constant number of profiles
  - Check if the profiles have a serializability violation
    - $O(kc^k)$  time – check all possible interleavings of profiles for serializability violations
- Recursive programs:  $O(n^3+kc^k)$  time
  - Extract profiles from each local thread using PDS reachability
    - $O(n^3)$  time
  - Check if profiles have a serializability violation  $O(kc^k)$  time

# Prediction with locking constraints

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- Consider a set of regular programs  $P_1 \parallel P_2 \parallel \dots \parallel P_n$
- Then it is *unlikely* that the atomicity prediction problem is solvable in time  $O(\text{poly}(n) \cdot f(k))$  for any function  $f$  !

i.e. we cannot remove the exponent  $k$  from  $n$

- How do we prove this?
  - Using parameterized complexity theory
  - The problem is  $W[1]$ -hard (with parameter  $k$ ).

# Prediction with locking constraints

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- **Parameterized complexity theory:**
  - Consider an algorithmic problem where input is of length  $n$ , but every instance has a parameter  $k$  associated with it.
  - A problem is fixed-parameter tractable (FPT) over parameter  $k$  if it is solvable in time  $O(\text{poly}(n) \cdot f(k))$  where  $f()$  is any function.
  - I.e. solved in a fixed-polynomial time in  $n$ , for any  $k$ .
- **$W[1]$ -hard problems**
  - No fixed-parameter algorithms known
  - Believed not to be FPT.
- **Example:**
  - Vertex cover is FPT in parameter  $k$ =number of colors
  - Independent-set is  $W[1]$ -hard in parameter  $k$  = number of sets

# Prediction with locking constraints

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- Prediction of atomicity violations in regular programs is  $W[1]$ -hard
- Hence an algorithm that runs in time  $O(\text{poly}(n) \cdot f(k))$  is unlikely (let alone an algorithm that runs linear in  $n$ ).
- Proof is by a (parameterized) reduction from the finite-state automata intersection problem (where the parameter is the number of automata), which is known to be  $W[1]$ -hard.
- **Note:**
  - Prediction of atomicity violations in straight-line programs is still open!
- Prediction of atomicity violations in recursive programs is undecidable
  - not surprising as locks can be used to communicate (Kahlon et al)

# Current and future directions

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- **Key project:**
  - Testing tool that executes alternate schedules that violate atomicity in order to find bugs.
  - More recent work has shown that nested locking yields tractable algorithms! (using ideas from Kahlon et al)
  - For non-nested locking, in practice, one can do more coarse analysis simply using locksets, and this yields reasonably good prediction algorithms.
- **Open problem:**
  - Atomicity for straight-line programs with locks still open.